## University of Nevada, Las Vegas Computer Science 456/656 Spring 2023

Review 1

1. True, False, or Open.
(a) _--_--- If $S$ is an infinite set, then $2^{S}$ must be uncountable.
(b) All standard arithmetic and matrix operations, as well as square root, are $\mathcal{N C}$.
2. Label each of the following sets as countable or uncountable.
$\qquad$ The set of integers.
$\qquad$ The set of real numbers.
_--------------- The set of rational real numbers.
_----_-_-_-_-_--- The set of irrational real numbers.
_-_-_-_-_-_-_-_ The set of binary languages.
_---------------- The set of co-RE binary languages.
---------------- The set of decidable binary languages.
---------------- The set of undecidable binary languages.
----------------- The set of unary languages.
_-_-_-_-_-_-_-_ The set of functions from integers to integers.
_-_-_-_-_-_-_-_ The set of recursive real numbers.
_---------------- The set of algebraic numbers.
A number is algebraic if it is a root of a polynomial with integral coefficients.
3. Each language class is closed under which operators? Write "T" or "F" in each cell.

|  | union | intersection | complement | concatenation | Kleene closure |
| ---: | :--- | :--- | :--- | :--- | :--- |
| regular |  |  |  |  |  |
| $\mathcal{N C}$ |  |  |  |  |  |
| context-free |  |  |  |  |  |
| $\mathcal{P}$-TIME |  |  |  |  |  |
| $\mathcal{N} \mathcal{P}$ |  |  |  |  |  |
| $\operatorname{co-} \mathcal{N P}$ |  |  |  |  |  |
| $\mathcal{P}-$ SPACE |  |  |  |  |  |
| recursively enumerable |  |  |  |  |  |
| co-recursively enumerable |  |  |  |  |  |
| undecidable |  |  |  |  |  |

4. Which of these problems, or languages, are known to be $\mathcal{N} \mathcal{P}$-complete? (Write T or F )
_-_-_-_TSP (traveling salesman)
_---_-_-_partition
------_-_block sorting
------_-equivalence of DFAs
------_-_equivalence of NFAs
-------_equivalence of regular expressions
-----_-_equivalence of regular grammars
------_-equivalence of context-free grammars
_-_-_-_-_Boolean circuit problem
------_-2SAT
------_-_3SAT
_-_-_-_-_4SAT
_------_generalized checkers (any size board)
_---_-_-_vertex cover
------_-_independent set
------_-dominating set
_--_-_-_integer factoring with binary numerals
_-_-_-_-_Rush Hour
------_Hex (the game)
------_Nim (the game)
5. Fill in the ACTION and GOTO tables for the grammar given below, with start symbol $E$.
6. $E \rightarrow E+{ }_{2} E_{3}$
7. $E \rightarrow E-{ }_{4} E_{5}$
8. $E \rightarrow-{ }_{6} E_{7}$
9. $E \rightarrow E *_{8} E_{9}$
10. $E \rightarrow\left({ }_{10} E_{11}\right)_{12}$
11. $E \rightarrow x_{13}$

|  | $x$ | + | - | $*$ | $($ | $)$ | $\$$ | $E$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 0 |  |  |  |  |  |  |  |  |
| 1 |  |  |  |  |  |  | halt |  |
| 2 |  |  |  |  |  |  |  |  |
| 3 |  |  |  |  |  |  |  |  |
| 4 |  |  |  |  |  |  |  |  |
| 5 |  |  |  |  |  |  |  |  |
| 6 |  |  |  |  |  |  |  |  |
| 7 |  |  |  |  |  |  |  |  |
| 8 |  |  |  |  |  |  |  |  |
| 9 |  |  |  |  |  |  |  |  |
| 10 |  |  |  |  |  |  |  |  |
| 11 |  |  |  |  |  |  |  |  |
| 12 |  |  |  |  |  |  |  |  |
| 13 |  |  |  |  |  |  |  |  |

6. Give a proof that the set of real numbers is uncountable.
