

University of Nevada, Las Vegas Computer Science 456/656 Spring 2024

Assignment 3: Due Friday February 16, 2024, 11:59 PM

Name: \_\_\_\_\_

You are permitted to work in groups, get help from others, read books, and use the internet. You will receive a message from the graduate assistant, Zachary Edwards, telling you how to turn in the assignment.

Recall that there is no such thing as the “set” of regular languages, only the “class” of regular languages. But if we pick an alphabet, we can have sets. For example, we can talk about the set of binary languages, the set of languages over the binary alphabet  $\{0, 1\}$ .

1. True or False, write T or F. If the answer is unknown to science at this time, write O, for Open.
  - (a) \_\_\_\_\_  $\mathcal{P}\text{-TIME} = \mathcal{NP}$ .
  - (b) \_\_\_\_\_  $\mathcal{P}\text{-TIME} = \mathcal{P}\text{-SPACE}$ .
  - (c) \_\_\_\_\_ Every  $\mathcal{NP}$  language is decidable.
  - (d) \_\_\_\_\_ The set of recursive real numbers is countable.
  - (e) \_\_\_\_\_ Every recursively enumerable language is decidable.
  - (f) \_\_\_\_\_ The problem of whether two context-free grammars are equivalent is recursively enumerable.
  - (g) \_\_\_\_\_ The set of all C++ programs is countable.
  - (h) \_\_\_\_\_ The set of recursively enumerable binary languages is countable.
  - (i) \_\_\_\_\_ The set of binary languages is countable.
  - (j) \_\_\_\_\_ If a CF grammar  $G$  is ambiguous, there cannot be any deterministic machine which constructs a parse tree for every string in  $L(G)$ .
  - (k) \_\_\_\_\_ The busy beaver function is recursive. (Look it up.)
  - (l) \_\_\_\_\_ The language  $\{a^n b^n c^n d^n : n \geq 0\}$  is context-sensitive.
  - (m) \_\_\_\_\_ There is a polynomial time algorithm for deciding whether a given Boolean expression is a contradiction. (An example of a contradiction is  $x*!x$ , where  $x$  is a variable of Boolean type and “\*” means “and.”)
  - (n) \_\_\_\_\_ The halting problem is decidable.
  - (o) \_\_\_\_\_ The halting problem is recursively enumerable.
2. State the pumping lemma for regular languages correctly.

3. For each of the grammars given below, each variable symbol is a capital Roman letter, each terminal symbol is a lower case Roman letter, and the start symbol is  $S$ .

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|---|---|
| (a) Which of these grammars generates $\{a^n b^n : n \geq 0\}$ ?              | Grammar $G_1$ :<br>$S \rightarrow aSb$<br>$S \rightarrow \lambda$   |
| (b) Which of these grammars generates $\{a^n b^m : n, m \geq 0, n \neq m\}$ ? | Grammar $G_2$ :<br>$S \rightarrow aA \mid Bb$<br>$A \rightarrow aA \mid aAb \mid \lambda$<br>$B \rightarrow Bb \mid aBb \mid \lambda$ |
| (c) Which two of these grammars are equivalent?                               | Grammar $G_3$ :<br>$S \rightarrow aSbS$<br>$S \rightarrow \lambda$  |
| (d) Which of these grammars are ambiguous?                                    | Grammar $G_4$ :<br>$S \rightarrow aSb$<br>$S \rightarrow SS$<br>$S \rightarrow \lambda$   |

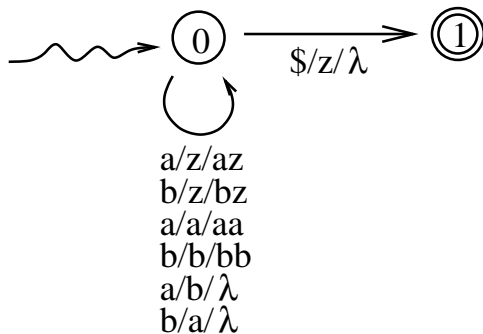
4. The correct order of the three labels on a transition of a PDA are written in this order: “read/pop/push.” Commas can be used instead of slashes.

When we push two or more symbols, the topmost one is on the left of the string. For example: if the label on the transition is  $a/z/az$ , then  $z$  is popped,  $a$  is read, and  $az$  is pushed, but that means  $z$  is pushed first, then  $a$  is pushed on top of it. A PDA transition must pop exactly one symbol, reads either zero or one symbol, and can push any number of symbols.

Assume that initially the stack is not empty, but contains just the bottom-of-stack symbol,  $z$ .

The input of a DPDA must end with the end-of-file symbol, which we write  $\$$ . The input of an NPDA does not need the end of file symbol, since it can correctly guess that it has reached the end.

- (a) What is the language accepted by the DPDA illustrated below?



- (b) Design a DPDA which accepts the Dyck language. For ease of grading, use the version where the terminal symbols are  $a$  and  $b$ , not parentheses.
- (c) The language  $L$  generated by the grammar  $S \rightarrow iS|iSeS|\lambda$  is ambiguous. Is there a DPDA that accepts  $L$ ? If so, draw it. If not, draw an NPDA that accepts  $L$ .
- (d) Draw a PDA which accepts the language of all palindromes over  $\{a, b\}$ . Your machine cannot be a DPDA, as you know. (Note: a palindrome can have odd or even length.)