## Computer Science 456/656 Spring 2007 Second Examination, April 12, 2007

No books, notes, scratch paper, or calculators. Use pen or pencil, any color. Use the rest of this page and the backs of the pages for scratch paper. If you need nore scratch paper, it will be provided.
The entire examination is 200 points.
1. True or False. [5 points each] In each blank space, write "T" if the statement is known to be true, "F" if the statement is known to be false, and "O" (for open) if it is not known to science at this time whether the statement is true.
(a) Every subset of a regular language is regular.
(b) There exists a machine <sup>1</sup> that runs forever and outputs the string of decimal digits of $\pi$ (the well-known ratio of the circumference of a circle to its diameter).
(c) For every real number $x$ , there exists a machine that runs forever and outputs the string of decimal digits of $x$ .
(d) If a language has an unambiguous context-free grammar, then there must be some DPDA that accepts it.
(e) The problem of whether two given context-free grammars generate the same language is decidable.
(f) The problem of whether a given string is generated by a given context-free grammar is decidable.
(g) The language $\{a^nb^nc^nd^n\mid n\geq 0\}$ is recursive.
(h) Let $L$ be the language over $\{a,b,c\}$ consisting of all strings which have more $a$ 's than $b$ 's and more $b$ 's than $c$ 's. There is some PDA that accepts $L$ .
(i) There exists a mathematical proposition that can be neither proved nor disproved.

<sup>&</sup>lt;sup>1</sup>As always in automata theory, "machine" means abstract machine, a mathematical object whose memory and running time are **not** constrained by the size and lifetime of the known (or unknown) universe, or any other physical laws. If we want to discuss the kind of machine that exists (or could exist) physically, we call it a "physical machine."

$^2$ .	Fill	the	blanks.	[5	points	${\rm each}$	blank]	
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- (a) An LALR \_\_\_\_\_\_ outputs a \_\_\_\_\_ derivation.
- (b) An  $\_$  of a language L is a machine that outputs all the strings of L and no other strings.
- 3. [20 points] State the pumping lemma for context-free languages.

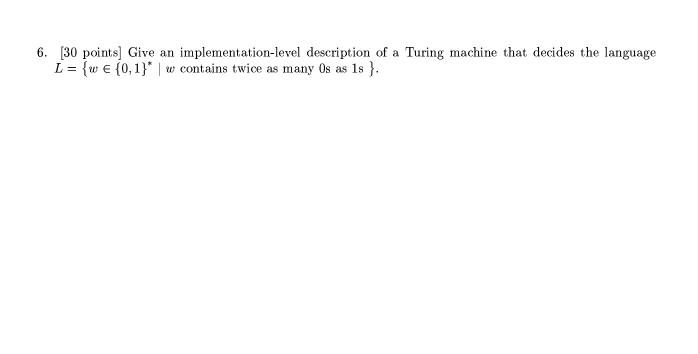
4. [30 points] State the Church-Turing thesis, and explain (in about 5 lines or less) why it is important.

## 5. [30 points]

- 1.  $S \rightarrow \epsilon$
- $2. S \rightarrow a_2 S_3 b_4 S_5$

	a	b	eof	S
0				1
1			halt	
2				
3		s4		
4		r1		
5				

Complete the ACTION and GOTO tables of an LALR parser for the grammar given above. This grammar unambiguously generates the "balanced parentheses" language, where a represents a left parenthesis, and b represents a right parenthesis. Example strings include  $\epsilon$ , ab, aabb, abab, and aabbab.



7. [30 points] What is the diagonal language? Give a brief sketch of the proof that it is not accepted by

any Turing machine. (If you use more than this page, you are writing too much.)