1. I will ask questions on the material in the fourth and fifth assignments, and also from the following material of this document.

2. One of the most commonly used search structures is unordered list. Even though you need linear search to find an item, the simplicity of the structure makes it useful for small sets of data.

A self-organizing list is a list where items are moved closer to the head if they are more frequently used. One standard method of self-organization is called move to front, where an item which is found is moved to the front of the list. This method is predicated on the “locality” assumption, that is, that items are not sought equally often, and it thus efficient to assume that if an item is sought, it is likely to be sought again.

Suppose that items are letters, and the list is QWERTYUIOP. When we execute find(I) the list becomes IQWERTYUIOP.

There is a more advanced method, called BIT. Initially, a random bit is placed at each item. When find(X) is executed, the bit is flipped, and item X is moved to the front if and only if its bit is 1.

For example, assume the list (with its bits) is initialized to be

```
0 1 1 1 0 1 0 0 0 1
Q W E R T Y U I O P
```

If we request find(T) followed by find(E), the list becomes

```
1 0 1 0 1 1 0 0 0 1
T Q W E R T Y U I O P
```

Here is another example. If the initial list is

```
0 1 1 1 0 1 0 0 0 1
Q W E R T Y U I O P
```

what is the list, with its bits, after executing these operations in this order?

find(R);
find(E);
find(P);
find(E);
find(I);
3. Walk through Kruskal’s algorithm to find the minimum spanning tree of the weighted graph shown below. Show the evolution of the union/find structure at several intermediate steps. Whenever there is choice between two edges of equal weight, choose the edge which has the alphabetically largest vertex. Whenever there is a union of two trees of equal weight, choose the alphabetically larger root to be the root of the combined tree. Indicate path compression when it occurs.
4. Construct an AVL tree by starting with an empty tree and then inserting the letters B,A,E,D,F,C in that order.

You can insert B,A,E,D,F without any rebalancing. But when you insert C, you will need to rebalance. Do you need a double rotation?

5. Let $A$ be a triangular array $\{A[i,j]\}$ where $0 \leq i \leq j \leq 5$. How many items are in the array? (Answer: 21) If $A$ is stored in RAM in row-major order, with base address 1024, where is $A[2, 3]$ stored? Assume each item uses one address of RAM.