## University of Nevada, Las Vegas Computer Science 477/677 Spring 2022

Answers to Assignment 3: Due Monday February 28, 2022, Midnight
Read the handouts sorting.pdf,

1. Fill in the blanks. One word per blank.
(a) The worst case number of comparisons during an execution of a comparison based sorting algorithm with an input of size $n$ is $\Omega(\log n!)=\Omega(n \log n)$.
(b) The items stored in a priority queue represent unfulfilled obligations.

A linked list has a head and a rear. Which of those will be the top, if linked list implements a stack? head.
2. Execute treesort by hand to sort the file MTHOYBKL.
(a) Create a binary search tree, inserting each item in the order given.







(b) Write the items in inorder. BHKLMOTY
3. Execute mergesort by hand with input file MTHOYBKL.

MTHOYBKL
MTHO YBKL
MT HO YB KL
MT HO BY KL
HMOT BKLY
BHKLMOTY
4. Execute heapsort with input file MTHOYBKL. Use array below. Add additional rows if needed.

Items in the sorted part are in boldface.

| M | T | H | O | Y | B | K | L |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| M | T | K | O | Y | B | H | L |
| M | Y | K | O | T | B | H | L |
| Y | M | K | O | T | B | H | L |
| Y | T | K | O | M | B | H | L |
| L | T | K | O | M | B | H | $\mathbf{Y}$ |
| T | L | K | O | M | B | H | $\mathbf{Y}$ |
| T | O | K | L | M | B | H | $\mathbf{Y}$ |
| H | O | K | L | M | B | $\mathbf{T}$ | $\mathbf{Y}$ |
| O | H | K | L | M | B | $\mathbf{T}$ | $\mathbf{Y}$ |
| O | M | K | L | H | B | $\mathbf{T}$ | $\mathbf{Y}$ |
| B | M | K | L | H | $\mathbf{O}$ | $\mathbf{T}$ | $\mathbf{Y}$ |
| M | B | K | L | H | $\mathbf{O}$ | $\mathbf{T}$ | $\mathbf{Y}$ |
| M | L | K | B | H | $\mathbf{O}$ | $\mathbf{T}$ | $\mathbf{Y}$ |
| H | L | K | B | $\mathbf{M}$ | $\mathbf{O}$ | $\mathbf{T}$ | $\mathbf{Y}$ |
| L | H | K | B | $\mathbf{M}$ | $\mathbf{O}$ | $\mathbf{T}$ | $\mathbf{Y}$ |
| L | H | K | B | $\mathbf{M}$ | $\mathbf{O}$ | $\mathbf{T}$ | $\mathbf{Y}$ |
| B | H | K | $\mathbf{L}$ | $\mathbf{M}$ | $\mathbf{O}$ | $\mathbf{T}$ | $\mathbf{Y}$ |
| K | H | B | $\mathbf{L}$ | $\mathbf{M}$ | $\mathbf{O}$ | $\mathbf{T}$ | $\mathbf{Y}$ |
| B | H | $\mathbf{K}$ | $\mathbf{L}$ | $\mathbf{M}$ | $\mathbf{O}$ | $\mathbf{T}$ | $\mathbf{Y}$ |
| H | B | $\mathbf{K}$ | $\mathbf{L}$ | $\mathbf{M}$ | $\mathbf{O}$ | $\mathbf{T}$ | $\mathbf{Y}$ |
| B | $\mathbf{H}$ | $\mathbf{K}$ | $\mathbf{L}$ | $\mathbf{M}$ | $\mathbf{O}$ | $\mathbf{T}$ | $\mathbf{Y}$ |
| $\mathbf{B}$ | $\mathbf{H}$ | $\mathbf{K}$ | $\mathbf{L}$ | $\mathbf{M}$ | $\mathbf{O}$ | $\mathbf{T}$ | $\mathbf{Y}$ |

5. Consider the array implementation of a stack of letters.

The bottom of the stack is in position 1.
(a) Show the structure after the following items have been pushed in this order: B, R, Y, E, M.

| 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: |
| B | R | Y | E | M |

5
5 is the location of the top of the stack.
(b) Show the structure after pop has been executed twice.

```
1 2 3 4 4 5
B R R Y E M
3
```

Popped items are not erased, since we are using "lazy delete." But the indicates that the top is in position 3. the stack now contains only 3 items, namely $\mathrm{B}, \mathrm{R}$, and Y , where Y is the top item.
6. In class we discussed three strategies for handling the false overflow problem for a queue implemented as an array. What were these strategies? (No more than three words to name each strategy. No need to give full explanations.)
slide
wrap
make array larger
7.


Write the depth first search traversal of the vertices of the directed graph $G$ shown here, then write the breadth first search traversal. In both cases use the alphabetic rule to break ties, so that everyone who works the problem correctly will have the same answer.

DF: sagurhkbmdeqcf
BF: sakgwbdrueqhcf
8. In the tiny Republic of Triland (pop 257) each citizen has a unique postal code consisting of three digits. Sort the following list of Trilandian postal codes using radix sort. Show the buckets at each phase.

Unsorted: 569045337192893450677190320537232554256512189121961300

| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 450 | 121 | 192 | 893 | 554 | 045 | 256 | 337 |  | 569 |
| 190 | 961 | 232 |  |  |  |  | 677 |  | 189 |
| 320 |  | 512 |  |  |  |  | 537 |  |  |

300
Concatenation: 450190320300121961192232512893554045256337677537569189

| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 300 | 512 | 320 | 232 | 845 | 450 | 961 | 677 | 189 | 190 |
|  |  | 121 | 337 |  | 554 | 569 |  |  | 192 |
|  |  |  | 537 |  | 256 |  |  |  | 893 |

Concatenation: 300512320121232337537845450554256961569677189190192893

| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 121 | 232 | 300 | 450 | 512 | 677 |  | 845 | 961 |
|  | 189 | 256 | 320 |  | 537 |  |  | 893 |  |
|  | 190 |  | 337 |  | 554 |  |  |  |  |
|  | 192 |  |  |  | 569 |  |  |  |  |

Concatenation: 121189190192232256300320337450512537554569677845893961
Sorted.

