Computer Science 302 Fall 2011 First Examination, September 22, 2011

	ge and the backs of the pages for scratch paper. If you need more scratch it will be provided.
The en	tire examination is 215 points.
1. True	e or False. [5 points each]
(a)	
(b)	$ \log(n^2) = O(\log n) $
(c)	Binary search on an ordered list of length n takes $O(\log n)$ time.
(d)	In the worst case, mergesort uses $O(n \log n)$ comparisons to sort n items
(e)	In the worst case, quicksort uses $O(n \log n)$ comparisons to sort n items
(f)	An abstract stack can hold any number of items.
(-)	
	in the blanks.
	in the blanks. [5 points] Any comparison-based sorting algorithm on a list of n items uses at least comparisons in the worst case. (Give an asymptotic answer.)
2. Fill	[5 points] Any comparison-based sorting algorithm on a list of n items uses at least
2. Fill (a)	[5 points] Any comparison-based sorting algorithm on a list of <i>n</i> items uses at leastcomparisons in the worst case. (Give an asymptotic answer.)
2. Fill(a)(b)	[5 points] Any comparison-based sorting algorithm on a list of <i>n</i> items uses at least comparisons in the worst case. (Give an asymptotic answer.) [5 points] The operation which inserts a new item into a stack is usually called

3. Using "Big O" notation state how many times "Hello world" will be printed for each of the pseudo-code fragments below, in terms of n. Give the best possible answer. For example, if you write $O(n^2)$ as the answer to (a), technically that is correct but it will be marked wrong because O(n) is a better answer.

```
(a) [0 points]
  for(int i=1; i<n; i++)
      cout << "Hello world" << endl;
(b) [20 points]
  for(int i=1; i<n; i++)
      for(int j=i; j<n; j++)
      cout << "Hello world" << endl;
(c) [20 points]
  for(int i=1; i<n; i++)
      for(int j=1; j<i; j=2*j)
      cout << "Hello world" << endl;
(d) [20 points]
  for(int i=1; i<n; i++)
      for(int j=i; j<n; j=2*j)
      cout << "Hello world" << endl;</pre>
```

4. [20 points]

Order the following functions by asymptotic class. Be sure to indicate which functions are in the same asymptotic class.

$$n,\, n^2,\, \log n,\, n\log n,\, n\log \log n,\, \log (n^2),\, \log^2 n,\, \sqrt{n},\, \frac{(2n+3)^4}{(n+2)^3},\, n!,\, \log (n!),\, 2^n,\, n^n,\, 3^n,\, 5n+\sqrt{n}+\log n+15$$

5. [20 points]

Using the stack algorithm given in class, evaluate the postfix expression

22*357+3-*+

showing the stack after each step. Each numerical input is a single digit; for example "22" is not twenty-two, but is rather the number two written twice. However, numbers on the stack can have any size.

- 6. [30 points] Suppose that the items of a queue Q are C, H, A, T in that order, meaning that C is the front item and T is the rear item.
 - (a) Sketch the appearance of a circular linked list implementation of Q, as we did in class (or in any other reasonable style).
 - (b) When you evaluate the function dequeue(Q), what will be the return value of that function?
 - (c) Show the appearance of the circular linked list after evaluating that function.
 - (d) After evaluating that function, execute enqueue(Q, E). Show the steps. (You should draw at least two additional figures.)

7. [20 points] **Challenge Problem.** Using "Big O" notation state how many times "Hello world" will be printed for the pseudo-code fragment below, in terms of n. Give the best possible answer, just as for Problem 3.

Warning: The purpose of this problem is to challenge the top students in the class. Do not attempt to work it unless you have answered all other questions and are satisfied with your answers.

```
for(int i=1; i<n; i=2*i)
  for(int j=i; j<n; j=2*j)
    cout << "Hello world" << endl;</pre>
```