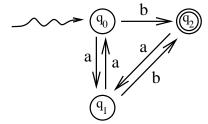
## University of Nevada, Las Vegas Computer Science 456/656 Fall 2025 Assignment 1: Due Saturday August 30, 2025, 11:59:59 PM

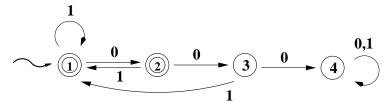
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You are permitted to work in groups, get help from others, read books, and use the internet. Turn in the assignment as instruced by the Teaching Assistant, Sabrina Wallace wallace4@cs.unlv.edu

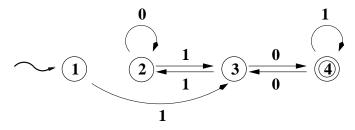
1. Let  $M_1$  be the DFA shown below.



Let  $M_2$  be the DFA shown below.



Let  $M_3$  be the DFA shown below.



Which of the following languages is accepted by  $M_1$ ? By  $M_2$ ? By  $M_3$ ?

- (a) The language of all binary strings in which every substring 00 is followed by 1.
- (b) All strings over  $\{a, b\}$  which end in b and which do not contain the substring bb.
- (c) The language of all binary numerals for positive integers equivalent to 2 modulo 3.
- (d) The language of all strings over  $\{a, b\}$  in which every b is followed by a.
- 2. Construct a DFA which accepts the language  $\{b^iab^j: i, j \geq 0\}$ , the language of all strings over  $\{a,b\}$  which contain exactly one a. Your figure need not show the dead state.

3.	Recall that $\emptyset$	is the empty	language. If I	L is some language,	what is the	concatenation $\emptyset L$ ?
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- 4. Let  $L_1 = \{\lambda\}$ . the language consisting of only the empty string. If  $L_2$  is some other language, what is the concatenation  $L_1L_2$ ?
- 5. Is concatenation of languages commutative? That is, is the equation  $L_1L_2 = L_2L_1$  always true?
- 6. Which of the following is true:
  - (a) If L is any language,  $L^0 = L$ .
  - (b) If L is any language,  $L^0 = \emptyset$ .
  - (c) If L is any language,  $L^0 = \{\lambda\}$ .

Hint: Think!

- 7. Does concatenation of languages distribute over union? That is, is  $L_1(L_2 + L_3) = L_1L_2 + L_1L_3$  always true?
- 8. What is  $\emptyset^*$ , the Kleene closure of the empty language?
- 9. True(T) or False(F).
  - i \_\_\_\_\_ Every language has a grammar.
  - ii \_\_\_\_\_ Every language is finite.
  - iii \_\_\_\_\_ 'Every language is infinite.
  - iv \_\_\_\_\_ Concatenation is commutative. That is,  $L_1L_2 = L_2L_1$  for any languages  $L_1$  and  $L_2$ .
  - v \_\_\_\_\_ Concatenation is associative. That is,  $(L_1L_2)L_3 = L_1(L_2L_3)$  for any languages  $L_1$ ,  $L_2$ , and  $L_3$ .
  - vi \_\_\_\_\_ The intersection of any two regular languages is regular.
  - vii \_\_\_\_\_ The complement of any regular languages is regular.
  - viii \_\_\_\_\_ The Kleene closure of any regular languages is regular.
- 10. The DFA  $M_1$  shown in Problem 1 is not minimal, that is, it is equivalent to a DFA with fewer states. Can you draw a state diagram of that DFA? Your figure need not show the dead state.