## University of Nevada, Las Vegas Computer Science 456/656 Spring 2022 Assignment 3: Due Monday March 7 2022

## Name:\_\_\_\_\_

You are permitted to work in groups, get help from others, read books, and use the internet. You will receive a message from our graduate assistant telling you how to turn in the assignment.

1. Which of the following Boolean expressions are satisfiable? Show the truth tables.

(a) 
$$x + ! x$$
 (b)  $x * ! x$ 

(c) 
$$(x + y) * (! x + ! y)$$
 (d)  $!(x \Rightarrow y) \Rightarrow ! y$ 

(e) 
$$!(z \Rightarrow (! x * y))$$
 (f)  $((x * ! y) * ! z) * (x \Rightarrow (y + z))$ 

2. Draw a diagram for a DPDA which accepts the language over  $\{a, b\}$  of all strings with equal numbers of a's and b's. Assume that the input string contains the end-of-file symbol .

- 3. Fill in the matrix below. Each answer is T or F, not O.
  - A Known to be  $\mathcal{P}$ -TIME.
  - B Known to be  $\mathcal{NP}$ .
  - C Known to be  $\mathcal{NP}$ -complete.
  - D Known to be  $co \mathcal{NP}$ .
  - E Known to be  $\mathcal{P}$ -space.
  - F Known to be decidable.
  - G Known to be undecidable.

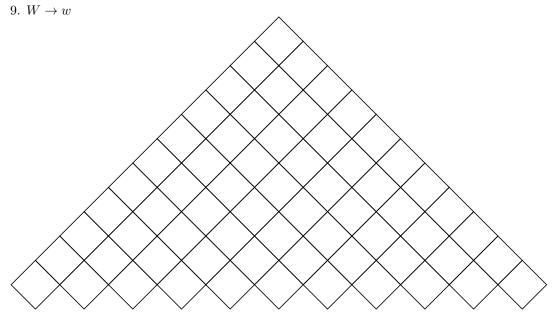
	A	В	С	D	Е	F	G
Regular grammar membership	Т	Т	F	Т	Т	Т	F
CF grammar membership							
CF grammar equivalence							
SAT	F	Т	Т	F	Т	Т	F
3-SAT							
2-SAT							
4-SAT							
Independent set							
Partition							
Knapsack							
Rush Hour							
co-Rush Hour							
Polygon placement							
Mover's problem							
Factoring							
Traveling Salesman							
DFA equivalence							
NFA equivalence							
Regular expression equivalence							
Halting problem							
Primality							

Definitions of some problems and languages.

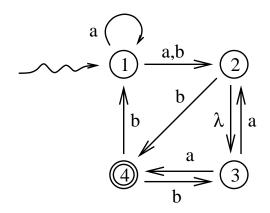
- Polygon placement. A given set of polygons can be placed in a given bigger polygon without overlap.
- Mover's problem. A given set of polygons, starting outside the room, can be moved into a room with a door, such that no overlap is permitted at any time during the move.
- Factoring. Given binary numerals  $\langle n \rangle$  and  $\langle a \rangle$ , n has a prime factor greater than a.
- Rush Hour. Given a configuration of the cars in a parking lot, the red car can be moved out.
- co-Rush Hour. Given a configuration of the cars in a parking lot, the red car cannot be moved out.
- Primality. A given binary numeral represents a prime number.

- 4. The following CF grammar generates all non-empty strings over  $\{a, b\}$  which have equal numbers of *a*'s and *b*'s. However, it is not CNF. Give a CNF grammar for the same language.
  - $S \to aSbS$
  - $S \to abS$
  - $S \to aSb$
  - $S \to ab$
  - $S \to bSaS$
  - $S \to bSa$  $S \to baS$
  - $S \rightarrow 0a$
  - $S \to ba$

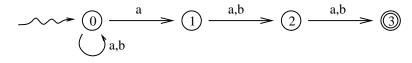
- 5. Use the CYK algorithm to decide whether the string *iwiiaewiaea* is generated by this CNF grammar by filing in the diagram below. Be sure to complete every cell.
  - 1.  $S \rightarrow a$
  - 2.  $S \rightarrow WS$
  - 3.  $S \rightarrow IS$
  - 4.  $S \to XY$
  - 5.  $X \rightarrow IS$
  - 6.  $Y \to ES$
  - 7.  $I \rightarrow i$
  - 8.  $E \rightarrow e$



6. Give a regular grammar for the language accepted by the following NFA.



7. Find a DFA equivalent to the following NFA. I was a mistake to give you problem 7 on the homework, since its solution is too complex. Insead, I am replacing it with a shorter version, below. The DFA should have 2<sup>4</sup> states (instead of 2<sup>5</sup> as before) but only half of those are reachable, so the resuling minimal DFA has 8 states.



8. Give a  $\mathcal{P}$ -TIME reduction of the subset sum problem to the partition problem.