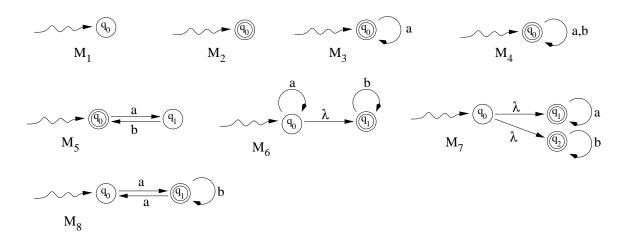
## University of Nevada, Las Vegas Computer Science 456/656 Spring 2025 Assignment 3: Due Saturday February 8, 2025, 11:59 PM

## Name:\_\_\_\_\_

You are permitted to work in groups, get help from others, read books, and use the internet. You will receive a message from the graduage assistant, Sepideh Farivar, telling you how to turn in the assignment.

- 1. Identify which machine accepts the language defined by each regular expression.
  - (a)  $a^* + b^*$  (e)  $a(aa + b)^*$ (b)  $\lambda$  (f)  $a^*b^*$
  - (c)  $a^*$  (g)  $(a+b)^*$
  - (d)  $\emptyset$  (h)  $(ab)^*$



- 2. True or False. If the answer is unknown to science at this time, write **O** for Open.
  - (a) \_\_\_\_\_ If L is any language, L + L = L
  - (b) \_\_\_\_\_ If L is any language,  $L \cap L = L$
  - (c) \_\_\_\_\_ If L is any language,  $\{\lambda\} \in L^*$ .
  - (d) \_\_\_\_\_ If L is any language, L + L = L
  - (e) \_\_\_\_\_ If L is any language,  $L \cap L = L$
  - (f) \_\_\_\_\_ If L is any language,  $\{\lambda\} \in L^*$ .
  - (g) \_\_\_\_\_ Any language consisting of all decimal numerals of an arithmetic sequence is regular.
  - (h) \_\_\_\_\_ Let L be a regular binary language. Let L' be the language of all strings obtained from members of L by substituting ab for 0 and c for 1. Then L' must be regular. For example, if  $L = \{0, 10, 10011\}$  then  $L' = \{ab, cab, cababcc\}$ .
  - (i)  $\mathcal{P}$ -TIME =  $\mathcal{NP}$ .

- 3. Let  $L_1 = \{a, ab\}$  and  $L_2 = \{a, ba\}$ . How many strings are there in the language  $L_1L_2$ ?
- 4. The following program decides whether a given integer n is prime.

```
Read n
For all i from 2 to n-1
If(n%i = 0) return False.
Return True.
```

At first glance you would say it is a polynomial time algorithm. But it isn't. In fact, it takes exponential time. Explain.

5. Any NFA with n states is equivalent to some DFA with at most  $2^n$  states, counting the dead state. Draw a DFA equivalent to the following three state NFA.

