University of Nevada, Las Vegas Computer Science 477/677 Spring 2025 Study for Examination April 9, 2025

1. True or False.

- (a) _____ If there are 100 data items and 200 possible hash values, a collision is so unlikely that you can, in practice, assume that it won't happen.
- (b) _____ If there are 100 data items and 10000 possible hash values, collisions are so unlikely that you can, in practice, assume that they won't happen.
- (c) _____ Open hashing uses open addressing.
- (d) _____ Open hashing uses probe sequences.
- (e) ______ You can avoid collisions in a hash table by making the table twice as large as the data set.
- (f) _____ False overflow for a queue can be avoided by implementing the queue as a circular list.
- (g) _____ If a stack is implemented as a linked list, the head of the linked list should hold the top item of the stack.
- (h) _____ Kruskal's algorithm uses dynamic programming.
- (i) _____ There will be no collisions if the size of a hash table is at least ten times the number of data items.
- (j) _____ A hash function should appear to be random, but cannot actually be random.
- 2. Solve each of these recurrences, giving an asymptotic answer.

(a)
$$F(n) = F(\log n) + 1$$

(b)
$$F(n) = F(5n/13) + F(12n/13) + n$$

(c)
$$F(n) = F(n-1) + 2F(n-2)$$

(d)
$$F(n) = F(\log n) + 1$$

(e)
$$F(n) = 5F(2n/3) + F(n/3) + 2n^4$$

(f)
$$F(n) = F(n/3) + F(2n/3) + 1$$

(g)
$$G(n) = 2G(n/4) + \sqrt{n}$$

(h)
$$H(n) = \log n + 1$$

(i)
$$H(n) = 4H(2n/5) + H(3n/5) + 2n^2$$

(j)
$$G(n) = 4(G(n/2) + 5n^2)$$

(k)
$$F(n) = F(n - \log n) + \log^2 n$$

(1)
$$F(n) = 4F(n/2) + n^2$$

(m)	$G(n) = G(4n/5) + G(3n/5) + n^2$			
(n)	T(n) = T(3n/10) + T(n/5) + n			
Fill	Fill in the blanks.			
(a)	In closed hashing, collisions are resolved by the use ofsequences.			
(b)	Name three kinds of search structurees.			
(c)	hashing, which can be used by a compiler to identify reserved words, does not have collisions.			
(d)	In closed hashing, if a collision occurs, a can be used to locate an unused position in the hash table.			
(e)	In a hash table, each item has two or more possible locations, and must be stored in one of those.			
(f)	Which of the following three statements is closest to the truth? (1) In SHA256 hashing, collisions are impossible. (2) In SHA256 hashing, collisions occur no more than once a year in practice. (3) In SHA256 hashing, collisions are so unlikely that industry experts claim they never occur.			
(g)	In an open hash table, there is a at each table index. Pick one of these answers: heap stack search structure			
(h)	A directed graph is defined to be if, given any two vertices x and y , the graph contains a path from x to y .			
(i)	A hash function fills the hash table exactly with no collisions.			
(j)	algorithm finds a binary code so that the code for one symbol is never a prefix of the code for another symbol.			
(k)	An acyclic directed graph with 9 vertices must have at least $____$ strong components. (Must be exact answer.)			
(1)	In there can be any number of items at a given index of the hash table.			
(m)	The asymptotic expected time to find the median item in an unordered array of size n , using a good			

3.

randomized algorithm, is _____

4. Write a recurrence for the time complexity of the code below, and solve that recurrence, giving an asymptotic function of n.

```
void george(int n)
{
   if(n > 1)
   {
     for(int i = 0; i < n; i++) cout << "hello" << endl;
     george(n/2); george((n+1)/2);
   }
}</pre>
```

- 5. A 3-dimensional $10 \times 20 \times 12$ rectangular array A is stored in main memory in column major order, and its base address is 1024. Each item of A takes two words of main memory, that is, two addressed location. Find the address, in main memory, of A[5][13][7].
- 6. You are trying to construct a cuckoo hash table of size 8, where each of the 8 names listed below has the two possible hash values indicated in the array. Put the items into the table, if possible. Instead of erasing ejected items, simply cross them out, so that I can tell that you worked it properly.

	h1	h2
Ann	1	0
Bob	4	2
Cal	0	7
Dan	1	6
Eve	1	0
Fay	6	2
Gus	5	3
Hal	3	7

7. Let $\sigma = x_1, x_2, \dots x_n$ be a sequence of numbers with both positive and negative terms. Write an O(n) time dynamic program which finds the maximum sum of any contiguous subsequence of σ . For example, if the sequence is -1, 4, -3, 2, 7, -5, 3, 4, -8, +6 then the answer is 4-3+2+7-5+3+4=12.

 $X[i] = \text{maximum sum of any legal subsequence of } x_1, \dots x_i$

 $Y[i] = \text{maximum sum of any legal subsequence which ends at } x_i$.

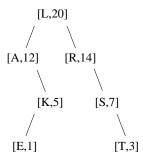
The program starts out as:

X[0] = 0

 $Y[1] = x_1$

etc.

8. The figure below shows a treap, where the data are letters and the nodes of the tree are memos, where the first component is the *key*, a letter, and the second component is a the *priority*, a random integer. Insertion of the letter G, where the priority is chosen (at random) to be 17. Show the steps.



- 9. Explain how to implement a sparse array using a search structure.
- 10. Consider the following C++ function.

```
int f(int n)
{
  if(n > 0)
    return f(n/2)+f(n/3)+f(n/6)+n*n;
  else
    return 0;
}
```

(a) The first of those subprograms is a recursive function. What is the asymptotic value of f(n)?

- (b) What is the asymptotic time complexity of the computation of f(n) using the recursive function?
- (c) What is the asymtotic time complexity of a computation of f(n) using memoization? (Hint: it's a power of log n.) ______
- 12. Find the time complexity of each of these code fragments in terms of n, using Θ notation.

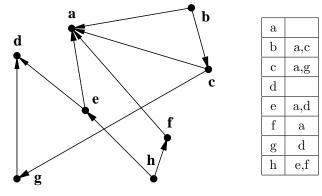
```
    (a) for(int i = n; i > 1; i = i/2)
        cout < "Hello world!";</li>
    (b) for(int i = 2; i < n; i = i*i)
        cout < "Hello world!";</li>
    (c) for(int i = 1; i < n; i++)
        for(int j = i; j < n; j=2*j)
        cout < "Hello world!";</li>
```

```
(d) for(int i = 0; i < n; i++)
    for(int j = n; j > i; j = j/2)
(e) for(int i = 0; i < n; i++)
    for(int j = i; j > 0; j = j/2)
```

- 13. Consider the function F computed by the recursive code given below.
 - (a) What is the asymptotic complexity of F(n)?
 - (b) What is the asymptotic time complexity of the recursive code when it computes F(n)?
 - (c) What is the asymptotic time complexity of a memoization algorithm which computes F(n)?

```
int F(int n)
{
  if(n < 3) return 1;
  else return F(n/3)+2*F((n+1)/3)+n*n;
}</pre>
```

- 14. If the array A[5][7] is stored in column-major order, how many predecessors does A[3][4] have?
- 15. You are implementing a 3D triangular array A where A[i][j][k] is defined for $0 \le k \le j \le i \le 4$, a total of 35 entries (Is that correct?), and is stored as a one-dimensional subarray of main memory in row-major order, with base address 1024. Each term of A takes one place in main memory. What would be the address, in main memory, of A[4][2][1]?
- 16. You are given an acyclic directed graph G = (V, E) where each arc has a positive weight. If (x, y) is an arc, we write w(x, y) for the weight of that arc. Describe a dynamic programming algorithm which calculates the directed path through G of maximum weight. (The weight of a path is defined to be the sum of the weights of its constituent arcs.) (Hint: your algorithm should use words such as "in-neighbor" or "out-neighbor.")
- 17. The directed graph shown below can be stored as an array of out-neighbor lists as shown.



Write the array of in-neighbor lists for the same graph.

18. Consider the following recursive C++ function.

```
int f(int n)
{
   if(n > 0) return f(n/2)+f(n/4)+f(n/4 + 1)+n;
   else return 0;
}
```

- (a) What is the asymptotic complexity of f(n) as a function of n, using Θ notation?
- (b) What is the asymptotic time complexity of the execution of this code as a sa an asymptotic function of n, using Θ notation?
- 19. Find the Levenshtein edit distance from the word "mennoover" to the word "maneuver." Show the matrix.
- 20. Here is another coin-row problem. You have a row of coins of various values, where the value of the i^{th} coin is V[i] > 0. Write pseudocode which finds the maximum value of a subset of coins, where the set may not contain coins which are either adjacent or just one apart in the row. That is, if the set contains the i^{th} coin, it may not contain either the $(i+1)^{st}$ coin or the $(i+2)^{nd}$ coin. For example, if the coins are (a) (b) (c) (d) (e) (f) (g) (h) in that order, the subset may be $\{(a), (d), (h)\}$, but not $\{(b), (d), (g)\}$.
- 21. Walk through the A^* algorithm to find the least cost path from S to T. The values of the heuristic function are indicated in red.

