

University of Nevada, Las Vegas Computer Science 477/677 Spring 2025

Assignment 1: Due Saturday January 31, 2026 23:59:59

Follow instructions given by our Graduate Assistant Rakibul Hassan [hassar2@unlv.nevada.edu](mailto:hassar2@unlv.nevada.edu) on how to turn in the assignment.

Name: \_\_\_\_\_

You are permitted to work in groups, get help from others, read books, and use the internet.

1. The sequence of powers of 2 is generated by the recurrence  $2^n = 2 \cdot 2^{n-1}$ . What is the recurrence which generates the Fibonacci sequence  $F_1, F_2, \dots$ ?
  
2. Write the sequence of all Fibonacci numbers under 100.
  
3. Which one of these statements is true?
  - (a) The Fibonacci numbers increase logarithmically.
  - (b) The Fibonacci numbers increase linearly.
  - (c) The Fibonacci numbers increase quadratically.
  - (d) The Fibonacci numbers increase exponentially.
  
4. Find the constant  $K$  such that  $F_n = \Theta(K^n)$ . What is the standard name of this constant?

5. Work Exercise 1 on the handout complexity.pdf.

(xxvi)  $\log 8$

(xxvii)  $\log_4 \sqrt{2}$

(xxviii)  $\log_3 9$

(xxix)  $\log_4 2$

(xxx)  $\log(\frac{1}{2})$

(xxxi)  $\log_3 \sqrt[3]{9}$

(xxxii)  $\log(\sqrt{8} - \sqrt{2})$

(xxxiii)  $2^{\log_4 25}$  (Yes, it's an integer!)

(xxxiv)  $\log \log \log \log 65536$

6. You've seen Landau notation. Originally, there was only "big O," but now there are several others. We will only use three of those this semester.

In each blank, write either  $\Theta$ ,  $O$ , or  $\Omega$ , using the following rules.

- Write  $\Theta$  if that is correct.
- If  $\Theta$  is not correct, write either  $O$  or  $\Omega$ , whichever is correct.

Hint:  $\log n$  grows more slowly than any polynomially increasing function of  $n$ .

(i)  $n \log n = \text{-----} (10n + \log(10n))$

(ii)  $\log(n^2) = \text{-----} (\log(n^3))$

(iii)  $10 \log n = \text{-----} (\log(n^2))$

(iv)  $n^{1.01} = \text{-----} (n \log^2 n)$

(v)  $n^2 / \log n = \text{-----} (n \log^2 n)$

This one requires serious thinking. Don't just write down the first thing that occurs to you.

(vi)  $n^{0.1} = \text{-----} (\log^2 n)$

The rest of these are harder, and may require calculation.

(vii)  $(\log n)^{\log n} = \text{-----} (n/\log n)$

(viii)  $\sqrt{n} = \text{-----} (\log^3 n)$

This one requires writing things down.

(ix)  $n^{1/2} = \text{-----} (5^{\log_2 n})$

Think!

(x)  $n2^n = \text{-----} (3^n)$

This one is (slightly) tricky.

(xi)  $2^n = \text{-----} (2^{n+1})$

This one is easy, if you think about it correctly.

(xii)  $n! = \text{-----} (2^n)$

Don't forget that the default base is 2.

(xiii)  $\log n^{\log_2 n} = \text{-----} (2^{(\log n)^2})$

If you know your calculus, this one is easy.

(xiv)  $\sum_{i=1}^n i^k = \text{-----} (n^{k+1})$

This next one is quite important for analyzing the time complexity of sorting algorithms, and it **will** appear on exams, and very likely during job interviews.

(xv)  $\log n! = \text{-----}, (n \log n)$

7. The C++ code below implements a function, "mystery." What does it compute?

```
float mystery(float x, int k)
{
    if (k == 0) return 1.0;
    else if (x == 0.0) return 0.0;
    else if (k < 0) return 1/mystery(x,-k);
    else if (k%2) return x*mystery(x,k-1);
    else return mystery(x*x,k/2);
}
```

8. Consider the following C++ program.

```
void process(int n)
{
    //cout << n << endl;
    if(n > 1) process(n/2);
    cout << n%2;
}

int main()
{
    int n;
    cout << "Enter a positive integer: ";
    cin >> n;
    assert(n > 0);
    process(n);
    cout << endl;
    return 1;
}
```

The last line of the output of `process(n)` is a string of bits. What does this bitstring represent?

9. Find the asymptotic time complexity of each code fragment, in terms of  $n$ . Use  $\Theta$  notation.

- (i) 

```
for(int i = 0; i < n; i++)
    cout << "Hello";
```
- (ii) 

```
for(int i = 1; i < n; i=2*i)
    cout << "Hello";
```
- (iii) 

```
for(int i = 0; i < n; i++)
    for(int j = 1; j < i; j=2*j)
        cout << "Hello";
```